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"Galactic Globular Cluster Infrared Fluxes"

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ABSTRACT

The goal of this research program was to measure the near infrared fluxes of selected bright galactic globular clusters, using the IRAS database. Graduate student Tyson has used IPAC facilities to process Additional Observations of eleven clusters, and 2D survey coadditions for a further eight clusters. All nineteen clusters were detected at 12 microns, while 13 were detected at 25 microns, and only one (47 Tuc) was detected at longer wavelengths. One and two dimensional King profile filters have been developed to optimize the signal to noise ratio of the cluster flux measurements. Detailed comparison with the infrared fluxes of early type galaxies will be undertaken once unpublished K band magnitudes have been obtained from a colleague.

1. INTRODUCTION

We are interested in whether the globular cluster 12µm fluxes exceed what is expected from photospheric emission alone. It would then be reasonable to associate the excess flux with intracluster, possibly circumstellar dust.

Evolutionary calculations (e.g. Rood 1973, Renzini 1981) indicate that globular cluster stars (mass $< 1 M_{\odot}$) at the turnoff) should lose about $0.2 M_{\odot}$ during the red giant phase and a further $0.1 M_{\odot}$ during second ascent. This mass loss seems to be required to fit the observed horizontal branch morphologies (Dupree 1986, Iben and Renzini 1983, Sweigart and Gross 1978).

Prior to IRAS the only observational evidence for mass loss in lower metallicity stars was the emission seen in the wings of H α (e.g. Cacciari and Freeman 1983,.Cohen 1976). However, Dupree, Hartman, and Averett (1984) use stellar atmosphere models to show that asymmetric H α lines can arise in the static chromospheres of population II giants, and thus mass loss rates could be $<< 2 \times 10^{-9} \, \text{M}_{\odot}/\text{yr}$, a factor of 20-50 less than for population I stars. We must therefore rely on the $12\mu\text{m}$ excess as solid evidence of mass actually lost, rather than the H α assymetry observed in the chromosphere of cluster giants. Frogel and Elias (1988), however, link significant near IR excess in clusters to the presence of luminous long period variables (LPVs). They also note that stellar pulsation will considerably increase, and possibly dominate the mass-loss rate over that predicted from the effects of radiation pressure alone.

Given the scarcity of information on mass-loss from population II giants and the importance of mass-loss both for the calculation of the late stages of stellar evolution, and the chemical enrichment of the Galaxy, the detection of excess IRAS flux is exciting. If mass-loss is radiation-pressure dominated then the appropriate rate can be estimated from following the momentum conservation method where $(dM_{gas}/dt) V_{\infty} = L_{IR}/c$ (e.g. Zuckerman 1986). If mass loss is pulsation-dominated then the process may be stochastic for any individual star. The very high mass-loss rates for LPVs inferred in Frogel and Elias (1988) suggest it may be better to characterize mass loss by averaging over an ensemble of globular clusters at a given metallicity thus allowing a statistical study of mass-loss in a well-defined sample of > 10^4 giants.

A second level of inquiry is to determine the mass-loss as a function of age and metallicity. For example, one expects mass-loss episodes in intermediate-age clusters. We now have a key opportunity to characterize the dependence. Rood (1973) found that such an effect could help explain cluster horizontal branch morphologies, while the results of Dupree, Hartmann, and Avrett (1984) indicate lower mass-loss rates in lower metallicity stars. The 34 target clusters of this study differ in metal abundance by nearly two orders of magnitude which should be sufficient to test the mass-loss dependence on metallicity.

The amount of stellar mass loss might also be found to depend on the horizontal branch type of the clusters. We have compiled for each cluster the parameter B/(B+R). Here B and R are the estimates of the number of blue and red horizontal branch stars seen in the cluster. Values range from zero to one, although this parameter might be best characterized through IUE observations. The connection between this parameter and mass loss arises from the fact that red horizontal branch stars have substantial convective envelopes whereas the blue stars are almost bare stellar cores. For stars of the same age, more mass must be shed during the red gant phase to make the blue horizontal branch stars. All other parameters being identical, one would assume that the giants in a cluster with a blue horizontal branch would be losing more mass at the first giant branch tip. Thus, there is strong suspicion that a correlation should exist between horizontal branch morphology and $12\mu m$ excess.

2. RESULTS

Tyson visited IPAC to use the IRAS data base in an attempt to detect $12\mu m$ and $25\mu m$ emission from 34 target globular clusters. This involved extensive interaction with M. Bicay of IPAC before, during, and subsequent to the visit.

IRAS additional observations (AOs) were available for eleven out of 34 clusters. Eight had full resolution 2D survey coadds available that were produced on IPACs older IBM main-frame. Two dimensional maps of the remaining fifteen were only available through the provisional "BIGMAP" IPAC software which processes the four IRAS bands only to the resolution of the 100µm detector. Tyson was told by IPAC support staff that full resolution two dimensional image reduction software should be available by March on their recently-acquired CDC Cyber computer.

Nineteen globular clusters were detected at $12\mu m$, of which five have definite $25\mu m$ emission (S/N > 5) and seven have possible $25\mu m$ emission (S/N < 2). Despite this success at $12\mu m$ and $25\mu m$ only 47Tuc has $60\mu m$ and $100\mu m$ emission. (See Gillett, et al. 1988). These detections represent every cluster for which either AOs or full resolution 2D coadds existed. The signal-to-noise for all of the low resolution BIGMAP coadds was ~1. We conclude that if full resulution 2D coadds were available for the balance of the clusters then positive detections would be likely.

Aside from the five globular clusters detected by Helfand and Applegate (private communiation, unpublished) this represents the *largest* reported sample of globular clusters detected by IRAS. While these nineteen detections are important, the intent of this study is to determine IR excess over what is to be expected from photospheric emission from cluster giants.

For the twelve clusters with 12 μ m and 25 μ m detections we can compare the 12-to-25 μ m flux ratio with that expected from the Rayleigh-Jeans relation $S_v \propto n^2$. Such a comparision reduces the sensitivity to the background noise subtraction. For pure stellar photospheres, the ratio is 4.3. A ratio less than 4.3 suggests the existence of warm intracluster dust; possibly circumstellar shells from RG mass loss. Notice from Table 2 that the flux ratio for four clusters is significantly *less* than 4.3. (The other clusters fall between 4.0 and 8.0.) These preliminary results provide confidence in the posibility of other clusters showing excess when we conduct the detailed analysis.

We are now ready to compare the $12\mu m$ and $25\mu m$ fluxes with existing near infrared and optical fluxes to determine a template spectrum for old population II stars. This is not a trivial task since similar IR fluxes are observed for a variety of V_{tot} . The 2.2-to-12 μm flux ratio will be compared to those already determined for stars in the bulge of our Galaxy (Frogel and Whitford 1987), the bulge of M31 (Soifer, *et al.* 1986), and early type galaxies. These estimates can be supplemented by the existing information on the luminosities and temperatures of individual giant stars which can be used to obtain alternative $12\mu m$ flux estimates.

Further refinement requires an application of the King function template. Once the cluster photospheric light is modelled, the flux profile is subtracted to reveal possible residuals which we may associate with IR emission from circumstellar dust. Due to limited time at IPAC Tyson could not apply the King function template to the clusters on location.

Now that Tyson has the data he will conduct this analysis over the next six months here at Columbia.

The cluster fluxes in Table 1 are provisional until a more detailed analysis of the stability of the background noise can be conducted; many estimates of the background were contaminated by bad pixels. Consequently, the reported fluxes are accurate to 20 percent but we ultimately expect to reduce the uncertainty to less that 10 percent based on what was achieved in Gillett, et al. (1988).

The manner in which Tyson obtained the integrated fluxes permits a 1D comparison with the King profile. Each cluster flux was measured through several (typically five or six) concentric apertures that ranged from slightly larger than the core radii up to ten core radii. This provides a radially dependent integrated cluster profile that can be compared with an appropriate King profile that has been convolved with the detector response function. For the brighter clusters, a 2D version of this profile comparision is available from Michael Bicay at IPAC. He has written software that computes the spatial correlation of emission between any two photometric bands (cf. Bicay, et al. 1989). Bicay has already run his 2D spatial correlation algorithm with the optical King profile on 47Tuc and he is currently running it on ω Cen. We have arranged that this analysis be conducted on the seven clusters with the largest angular extent.

In March, full resolution survey coadds for all four IRAS bands will be available through the modified and improved BIGMAP software. The 15 clusters for which AOs and full resolution 2D coadds were not available during Tyson's latest trip to IPAC will be run at that time.

At IPAC, M. Melnyck is developing specialized code based on the Richardson-Lucy 2D mapping algorithm that reconstructs the individual IRAS scans to obtain resolution that is three times better than what is quoted for the band-averaged detector profiles. Tyson has been encouraged by the support staff to return to IPAC in October 1990 when this software is expected to come on line. Two dimensional coadds at three times the current resolution will permit us to characterize the cluster structure as well as the total cluster emission. In particular, the correspondence of any intracluster dust with the stellar component will help to determine whether indeed intracluster dust represents circumstellar shells from RG mass loss or dust accretion from successive passes through the Galactic disk. It will also help to isolate individual sources within the cluster which may not be centrally distributed (e.g. Gillett, et al. 1986).

The successful $12\mu m$ detections reported herein suggest exciting future paths:

- 1) Extend the current work to include IRAS photometry of *all* globular clusters in the Galaxy.
- 2) Conduct high resolution IRAS photometry on the Magellanic cloud globular clusters.
- 3) To simultaneously address the same questions from a different wavelength we note that for stars with extreme mass loss we expect blue stellar cores. In particular, high mass loss at the AGB tip would produce blue stars without an obscuring envelope. If the process is rapid, the cluster's horizontal branch morphology can be altered significantly by a change in the relative frequency of red to blue giants.

Table 1: GLOBULAR CLUSTER DETECTIONS

Band 1 Band 2 Band 3 Band 4 Band 2 Band 3 Band 4 Band 3 B	NCC	Name	Aperture 1	Aperture 2	Aperture 3	Aperture 4	Aperture 5	Aperture 6	Rc	Vtot	[Fe/H]	B/(B+R)
12mm 0.831 2.035 2.235 0.221 10.485 12.077 1.000 1.000 0.146 0.224 0.252 0.332 0.325 0.3		Band 2: Band 3:	,	•	•	·	•					
Sum	104	47 Tuc	2.400	4.200	6.000	7.800	12.000	,	0.39	3.83	-0.71	o
Goum 0.146 0.224 0.252 0.332 0.325		12um	3.105	7.230	9.291	10.485	12.077					
100um 0.213 0.419 0.661 1.176 2.041		25um	0.831	2.035	2.755	3.106	3.696					
120m		60um	0.146	0.224	0.252	0.332	0.325					
12um 25um 0.019 0.282 0.567 0.749 0.861		100um	0.213	0.419	0.661	1.176	2.041					
25um	362								0.21	6.46	-1.27	0.05
12m							0.881					
12um 0.297 0.445 0.446 0.298 1.413		25um	0.005	0.081	0.211	0.389	0.860					
Sam	3201		2.400	3.000	4.800		7.200		1.09	6.68	-1.61	0.54
139 WCen 120m 0.610 3.462 5.400 7.200 10.200 2.62 3.52 -1.59 0.95		12um	0.297	0.445	0.846	0.988	1.413					
12mm		25um	0.063	0.092	0.194	0.237	0.355					
12m	5139	w Cen	1.800	4.200	5.400	7.200	10.200		2.62	3.52	-1.59	0.95
25um												
12um												
12um	5272	мз .	1 200	1 800	4 200	6 000	10 200		0.42	5.02	.1 66	0.55
12um	3212								0.42	3.92	-1.00	0.55
12um	5004	Me	1 200	1 000	2 000		40.000	12 222	0.44	F 60		0.76
6121 M4 12um 1.146 2.883 4.964 8.005 12.492 16.223 5.76 -1.33 0.44 12um 1.146 2.883 4.964 8.005 12.492 16.223 1.23 5.76 -1.33 0.44 12um 1.146 2.883 4.964 8.005 12.492 16.223 1.23 5.76 -1.33 0.44 12um 1.000 1.0006 0.364 0.929 1.229 1.798 1.798 25um 0.021 0.085 0.227 0.335 0.335 0.335 1.78 1.798	5904								0.44	5.69	-1.4	0.76
12um												
1.000	6121								1.23	5.76	-1.33	0.44
12um 25um 0.096 0.364 0.929 1.299 1.798		120111	1.140	2.003	4.504	8.003	12.452	10.223				
25um	6205	M13	1.000	2.400	4.800	7.800	13.200		0.83	5.68	-1.65	1
6218 M12 1.000 2.500 4.000 6.000 9.000 15.000 1.18 6.77 -1.61 0.95 25um 0.032 0.061 0.066 0.887 1.035 1.035 1.18 6.77 -1.61 0.95 25um 0.032 0.061 0.061 0.887 1.035 1.035 1.18 6.77 -1.61 0.95 0.95 0.032 0.061 0.061 0.061 0.0867 1.035 1.035 1.067 0.070 6.55 -1.6 0.94 0.001 0.032 0.061 0.06			0.096	0.364	0.929	1.299	1.798					
12 m 25 m 0.071 0.362 0.606 0.867 1.035 1.167		25um	0.021	0.085	0.227	0.335	0.335					
25um 0.032 0.061 6254 M10 1.000 2.000 3.000 5.000 0.70 6.55 -1.6 0.94 25um 0.026 0.1112 0.203 0.251 6266 M62 0.750 1.500 2.250 3.000 5.000 7.000 0.24 6.68 -1.28 6267 M2 0.366 1.222 2.111 2.950 5.068 7.018 6341 M92 0.500 0.28 0.306 0.366 6341 M92 0.500 0.167 6388 0.500 1.000 2.000 3.000 4.000 6.000 0.15 6.73 -0.74 6388 0.500 1.000 2.000 3.000 4.000 6.000 0.15 6.73 -0.74 6388 0.12um 0.171 0.577 1.513 2.389 3.059 3.923 1.062 6397 12um 0.171 0.577 1.513 2.389 3.059 3.923 1.062 6597 12um 0.150 0.522 0.847 1.380 1.793 2.194 6541 0.600 1.800 3.000 4.200 6.000 0.78 5.75 -1.91 0.91 6541 12um 0.000 2.000 3.000 4.200 5.000 6.000 0.78 5.75 -1.91 0.91 6541 12um 0.000 0.008 0.146 0.360 0.538 0.694 0.709 6752 12um 0.077 0.615 0.987 1.426 1.632 1.635 7078 M15 0.600 1.800 4.200 6.000 1.632 0.694 0.709 6752 12um 0.177 0.615 0.987 1.426 1.632 1.635 7078 M15 12um 0.011 0.192 0.560 0.617 0.000 1.630 0.49 5.48 -1.54 1 7078 M15 12um 0.011 0.192 0.560 0.617 0.000 0.009 6.02 -2.15 0.81 7078 M15 12um 0.011 0.192 0.560 0.617 0.000 0.71 0.000 0.71 7.00 0.000 0.71 0.000 0.71 0.000 0.0	6218	M12	1.000	2.500	4.000	6.000	9.000	15.000	1.18	6.77	-1.61	0.95
6254 M10 1.000 2.000 3.000 5.000		12um	0.071	0.362	0.606	0.867	1.035	1.167				
12um 25um 0.138 0.448 0.755 1.118 0.203 0.251		25um	0.032	0.061								
12um 25um 0.138 0.448 0.755 1.118 0.203 0.251	6254	M10	1.000	2.000	3.000	5.000			0.70	6.55	-1.6	0.94
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25um									0.24	0.00	1.20	•••
12um		1					5.000	7.010				
12um	6341	Mos	0.500									0.07
12um	0341								0.31	6.39	-2.24	0.97
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12um												
12um				0.141	0.007	0.550	0.030	1.002				
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12um		12Um	0.150	0.522	0.847	1.380	1.793	2.194				
12um	6541	1	0.600	1.800	3.000	4.200	6.000	10,200	0.28	6.08	-1.83	0.94
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12um 25um 0.011 0.192 0.560 0.617 0.005 0.072 0.086 1851 0.600 1.200 1.800 4.200 25um 0.011 0.084 0.169 0.341 0.600 1.800 3.000 4.800 7.200 9.000 0.14 7.19 -0.59 12um 0.049 1.474 6.304 17.276 36.716 44.672	707A	M15	0.600	1 000	4 200	c 000			A 45	e 00	2 4 5	0.04
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25um 0.011 0.084 0.169 0.341 6441 0.600 1.800 3.000 4.800 7.200 9.000 0.14 7.19 -0.59 12um 0.049 1.474 6.304 17.276 36.716 44.672	. 0.5 -	- 1										
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12um 0.049 1.474 6.304 17.276 36.716 44.672	6441	- 1	0.600	1.800	3.000	4.800	7.200	9.000	0.14	7.19	-0.59	•••
²⁵ um 0.008		1	0.049	1.474	6.304	17.276	36.716					
		25um	0.008	0.164	0.680	3.745	19.530	28.031				

Table 2: Flux Ratios

NGC	Name	12um/25um
104	47 Tuc	3.3
362		1.0
3201		4.0
5139	Omega Cen.	3.3
6205	M13	5.4
6218	M12	5.9
6254	M10	4.4
6266	M62	8.0
6388		3.7
6752		5.5
7078	M15	6.5

Notes to Table 1

- Apertures (in bold) are radii in arc minutes
- Rc is the core radius in arc minutes from Madore (1980).
- Vtot are total visual magnitudes from Webbink (1985).
- Metal abundances [Fe/H] are from Zinn and West (1984).
- Horizontal Branch types B/(B+R) are from Zinn (1980).
- There was possible contamination from a nearby source in the flux levels for NGC 6441

Notes to Table 2

The flux ratios are taken from the largest aperture where the 25 μ emission can be distingushed from background noise (S/N > 2).

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